

*Progressive Education Society's*  
Modern College of Arts, Science and Commerce (Autonomous),  
Shivajinagar, Pune - 5

Department Of Mathematics  
**SYBSC (Semester IV) 19ScMatU403**

Based on Vector Calculus

Subject : Mathematics Practical-IV (19ScMatU403)

Practical Incharge: Rima Ahuja

**Practical 5: Surface Integral And Stoke's Theorem**

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1. If  $\vec{f} = 18z\hat{i} - 12\hat{j} + 3y\hat{k}$  and  $s$  is part of plane  $2x + 3y + 6z = 12$  in the first octant then evaluate  $\iint_S \vec{f} \cdot \vec{n} \, ds$ .
2. ' $S$ ' is the closed surface bounded by the planes  $z = 0$  and  $z = 1$  and cylinder  $x^2 + y^2 = 4$  then evaluate  $\iint_S x^3 \, dy \, dz + x^2 \, dz \, dx + x^2 z \, dx \, dy$ .
3. Verify stokes theorem for  $\vec{f} = (xy)\hat{i} + (xy^2)\hat{j}$  and ' $C$ ' is boundary of the square vertices  $(1, 0), (-1, 0), (0, 1), (0, -1)$  in xoy plane.
4. Use Stokes theorem to prove that  $\int_C \sin z \, dx - \cos x \, dy + \sin y \, dz = 2$  and ' $c$ ' is boundary of the rectangle  $0 \leq x \leq \pi, 0 \leq y \leq 1, z = 3$ .
5. Verify stokes theorem for  $\vec{f} = (2x - y)\hat{i} - yz^2\hat{j} - y^2z\hat{k}$  and the surface  $s$  of plane  $x^2 + y^2 + z^2 = 1$  in the upper half.